Performance of classic multiple factor analysis and model fitting in crop modeling

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Abstract: Multivariate statistical analysis and regression, which are typical methods for crop modeling, have direct influence on the accuracy of model, but the applications of these methods usually depend on experiences. In this research, the performances of some common methods of statistical analysis and regression model were compared and verified, in order to avoid the blindness in crop modeling. The monitoring data of growth environment and photosynthesis of tomato, pumpkin and cucumber were obtained by PTM-48A. For the object variable of CO₂ exchange rate, selectivity on the main environmental factors by correlation analysis and path analysis were quantitatively compared. The performances of four kinds of multivariate binomial regression equations were compared using a comprehensive aggregative indicator, and the effectiveness of modeling was verified with the selected optimized multivariate statistical analysis and regression equation. Results showed that path analysis was more comprehensive and effective than correlation to discrimination of the variables, especially the path analysis ruled out some suspected independent variables which were not really independent, and the pure quadratic was more suitable to crop modeling because of its simple structure and high accuracy when the data set was small. The conclusion of this research has a general applicability, and offers a useful reference and guide for the other study and application of crops' modeling.

Keywords: crop model, multivariate statistical analysis, path analysis, regression, comparison

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1 Introduction

Crop model was one of the core technologies supporting the Precision Agriculture, and it was also the essential part of the intelligent production[1]. Crop model was to obtain accurately of growth environmental factors and physiological parameters, and to indicate quantitatively the relationship of them[2]. The typical crop models are DSSAT (Decision Support System of Agricultural Technology Transfer), APSIM (Agricultural Production Systems sIMulator), CERES (Crop and Environment Research Synthesis), and so on[3]. Because of the difference of growth condition, location and variety, every crop model has its own adaptation and target. Based on the specific conditions, the universal model should be improved to satisfy the actual demand. The improved process not only demands the complete agriculture knowledge, but also needs high-level mathematics and computer resources. So the application of typical crop model is not applied widely, and the small sample size dedicated crop model for the actual demand is common in practice.

To build up a crop model, firstly the independent variables and dependent variables, which have large

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influence on the object variable of model, should be selected using methods of multivariate statistical analysis, using the professional data process tools like Excel, SPSS, and SAS. Then regression model or the other models should be used to build up the crop model. The practicality and accuracy of model should be verified, using the test data to predict the unknown variable. The common multivariate statistical analysis includes standard correlation analysis\(^4\), principal components analysis\(^5\), path analysis\(^6\), and so on. Regression analysis is generally used in mathematical modeling. But the independent variables and form of equation are always chosen by experience. And empirical equations are often multitude and inconsistent\(^7\). The existing small sample size crop model is well-directed but has low adaptability. Although the model has high accuracy, the multivariate statistical analysis and regression model are selected according to the experience, instead of the quantification comparison results of the methods\(^8\). The empirical and blind selection becomes the hindrance of application and development of model\(^9\), which is also the difficulty of agricultural informatics. The methods of multivariate statistical analysis and regression have been compared and verification in the previous study\(^10\), but the experiment and expression of selecting the optimal method were not convincing enough.

In this research, methods of multivariate statistical analysis and regression were compared, using the preprocessed monitoring data of growth environment and photosynthesis of the tomato, pumpkin and cucumber. By the methods of correlation analysis and path analysis, the environmental characters impacting CO\(_2\) exchange were picked out to put the analysis methods into comparison. The regression equations were found to compare the equations in respects of complexity and accuracy. The data of cucumber were used to verify the optimum multivariate statistical analysis and regression equation.

2 Materials and methods

2.1 Experimental data

In this research, three common outdoor vegetables, including tomato, pumpkin and cucumber, were continuously monitored for at least 24 hours, by using the PTM-48A photosynthesis monitor of B.F. Agritech Company\(^{11,12}\), expecting to obtain the data of their photosynthetic physiological characteristic and growth environment. Figure 1 shows that the photosynthetic physiology and environmental factors online monitoring system includes five modules: the LC-4B leaf chambers, the multiple environmental factors sensors, the system console, the communication module and computer\(^{13}\).

The system console controls the LC-4B leaf chamber open and close. If the LC-4B leaf chamber is closed, the system console will detect the LC-4B leaf chamber’s concentration of carbon dioxide. After calculating, the system console obtains leaf’s CO\(_2\) exchange rate and transpiration rate. In addition, the system console is connected to the air temperature and humidity sensor, leaf’s temperature and humidity sensor, soil moisture sensor, light radiation sensor and other environmental factor sensors. The data of real-time photosynthetic physiology and environmental parameters are stored in the system console. Through the RS232 serial port or
the wireless communication module, the system console transfers the data to a computer. The system console makes four LC-4B leaf chambers alternately opened and closed. Each closing time is 30 s, which is the detection time. Each opening time is one minute. During this time, the CO₂ absorber column will absorb the excess carbon dioxide in the console. When the four LC-4B leaf chambers’ detections are completed, the system console will transfer the data to a computer. The monitoring time interval was uniform and set to 30 min, and the air flow was set to 0.84 LPM.

PTM-48A can obtained data of 31 variables for single monitor. The monitored data can be divided into two parts, the first part of which was the data of four leaves’ physiological characteristic, and the rest was the ambient environmental parameters. There were eight environmental variables in all. We picked out the average value of four leaves’ CO₂ exchange rates as the object variable, and the eight ambient environmental parameters as independent variables to study the influence of growth environment on the CO₂ exchange rate of crop. In order to decrease the amount of experimental work and study the physiological change of the whole crop, we took the average physiological value of four leaves as the physiological data of the whole crop. Eight environmental factors which were the independent variables, were summarized as follow: Air Temperature $T_a$ (°C), Relative Humidity $R_h$ (%RH), Radiation $R_a$ (micromole/m²·s), Absolute Humidity $A_H$ (g/m³), CO₂ concentration in the air $C_{CO₂}$ (ppm), Vapour Pressure Deficit $V_{pd}$ (kPa), Dew Point $D_p$ (°C), Atmospheric Pressure $P_a$ (mbar), defined as $X_1- X_8$. The CO₂ Exchange $E$ (micromole/m²·s) was defined as the dependent variable $Y$.

2.2 Analysis methods

The analysis and process of experimental data was as Figure 2.

At first, the monitoring data was preprocessed to convert the output table into the table which the processing software can read. Then Chauvenet’s criterion and linear smoothing algorithm were used to check and process outlier. Forty-eight groups of data in 24 hours were chosen from the physiological and environmental data of the tomato and pumpkin as the experimental samples. The experimental samples were used for methods comparison, and the data of cucumber was for verification. The cucumber’s data were divided into two parts, the first 48 groups of which were sampled data for modeling, and the rest were test data for predicting.

The preprocessed data were multivariate analyzed, using two methods, namely the correlation analysis and path analysis, for the purpose of getting the environmental factors that affect the rate of CO₂ exchange. In addition, the two methods were compared. In this research, the Person simple correlation coefficient\[^{14,15}\] was adopted to indicate the relation between variables\[^{16}\].

\[
R_y = \frac{C_y}{\sqrt{C_y C_y}}
\]  

(1)

where, $C_{ij} = \text{cov}(x_i, x_j)$ is the covariance of $x_i$ and $x_j$. The effect of environmental factors on CO₂ exchange is expressed by the direct path coefficient $\rho_i$ ($i=1, 2, ..., n$), which is calculated as follow\[^{17}\]:

\[
\begin{bmatrix}
\rho_1 \\
\rho_2 \\
\vdots \\
\rho_n
\end{bmatrix} =
\begin{bmatrix}
c_{11} & c_{12} & c_{13} & \cdots & c_{1n} \\
c_{21} & c_{22} & c_{23} & \cdots & c_{2n} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
c_{n1} & c_{n2} & c_{n3} & \cdots & c_{nn}
\end{bmatrix}
\begin{bmatrix}
r_{11} \\
r_{12} \\
\vdots \\
r_{1n}
\end{bmatrix}
\]  

(2)

where, $n$ is the number of independent variables; $y$ is the dependent variable, $r$ is the correlation matrix, and $c = r^{-1}$ was the invertible matrix of $r$. The indirect path coefficient $b_{ij}$ is the product of the direct path coefficient and correlation coefficient, indicating the
influence of independent variable \(x_i\) on dependent variable \(y\) through \(x_j\).

The direct path coefficient \(\rho_{ij}\) \((i=1, 2, \ldots, n)\) in Equation (2) was also the partial regression coefficient. And for \(N\) groups of data, the significance test statistics of path coefficient \(F\) was computed as Equation (3)\(^{[18]}\).

\[
F = \frac{\sum_{j=1}^{n} \rho_{ij}^2 / c_{ij}}{(N-n-1)}
\]

Regression analysis was carried out, regarding the analyzed environmental factors as independent variables and the CO\(_2\) exchange as a dependent factor. After determining the independent and dependent variables, the suitable model should be selected. Then the coefficients could be calculated by the least square method, according to the historic statistics. The multivariate binomial regression includes linear, pure quadratic, interaction and quadratic.

**Linear:**

\[
y = \beta_0 + \beta_1x_1 + \cdots + \beta_mx_m
\]

**Pure quadratic:**

\[
y = \beta_0 + \beta_1x_1 + \cdots + \beta_mx_m + \sum_{i \leq j < m} \beta_{ij} x_i x_j
\]

**Interaction:**

\[
y = \beta_0 + \beta_1x_1 + \cdots + \beta_mx_m + \sum_{i < j < m} \beta_{ij} x_i x_j
\]

**Quadratic:**

\[
y = \beta_0 + \beta_1x_1 + \cdots + \beta_mx_m + \sum_{i \leq j < m} \beta_{ij} x_i x_j
\]

In order to pick out the optimal regression model, an aggregative indicator in Equation (8) was put forward, taking account of two aspects including accuracy and complexity comprehensively.

\[
G = a_1RMSE + a_2MAE + a_3R^2 + a_4N_b
\]

where, \(\tilde{RMSE}\), \(\tilde{MAE}\), \(\tilde{R^2}\) and \(\tilde{N_b}\) are the data of \(RMSE\), \(MAE\), \(R^2\) and \(N_b\) by normalization operation. \(RMSE\), \(MAE\), and \(R^2\) are calculated as follows:

\[
RMSE = \sqrt{\frac{\sum_{i=1}^{n} (OBS_i - SIM_i)^2}{n}}
\]

\[
MAE = \frac{\sum_{i=1}^{n} |OBS_i - SIM_i|}{n}
\]

\[
R^2 = \frac{SSR}{SST} = \frac{SSR}{SSE + SSR} = \frac{\sum_{i=1}^{n} ((\sum_{j=1}^{n} OBS_j/n - SIM_i)^2)}{\sum_{i=1}^{n} (OBS_i - SIM_i)^2 + \sum_{i=1}^{n} ((\sum_{j=1}^{n} OBS_j/n - SIM_i)^2)}
\]

In Equations (9)-(11), \(n\) is the number of samples, \(OBS_i\) is the observed value, and \(SIM_i\) is the simulated value.

\(RMSE\) (Root Mean Square Error), is the standard error\(^{[19]}\), and \(MAE\) (Mean Absolute Error), is an average of absolute errors. \(R^2\) (R-square) is the coefficient of determination ranged from 0 to 1, and the nearer the \(R^2\) approaches 1, the stronger explanatory ability was, and the better performance of the model was. \(N_b\) is the number of polynomial coefficients of each regression equation. \(RMSE\), \(MAE\), and \(R^2\) can reflect the accuracy of model and complexity is smaller if \(N_b\) is smaller. To take both accuracy and complexity into consideration, set \(a_1\), \(a_2\), \(a_3\), \(a_4\) to \(\frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{2}\). And if \(G\) is smaller, the model is better.

Using the optimal method of multivariate analysis, the modeling data of cucumber was analyzed and the regression model was developed. Practicability and accuracy was verified and the results were compared with that of other prediction models.

### 3 Results and discussion

#### 3.1 Multivariate analysis of tomato and pumpkin

Eight environmental factors which were the independent variables, were summarized as follow: Air Temperature \(T_a\), Relative Humidity \(R_h\), Radiation \(R_a\), Absolute Humidity \(A_h\), CO\(_2\) concentration in the air \(C_{CO2}\), Vapour Pressure Deficit \(Vpd\), Dew Point \(D_p\), Atmospheric Pressure \(P_a\), defined as \(X_1\) to \(X_8\). The CO\(_2\) Exchange rate \(E\) is defined as the dependent variable \(Y\). In Table 1, the Person correlation coefficients between CO\(_2\) exchange and its impact factors were calculated from Equation (1). In Table 1, the upper halves of cells are the correlation coefficients of factors in tomato, and the lower halves are those in pumpkin.
As shown in Table 1, there are six environmental factors greatly affecting the $E$ of tomato, including $T_a$, $R_{HF}$, $R_v$, $C_{CO_2}$, $V_{pd}$ and $D_p$. Besides of the five factors, $A_{HF}$ also expressed a highly significant correlation with $CO_2$ exchange. While all environmental factors showed greatly significant correlation with $E$ in pumpkin. The variables such as $T_a$, $R_{HF}$, $A_{HF}$, $V_{pd}$ and $D_p$ were chosen as independent variables, but these variables were not really independent, and that might lead to unnecessary complication of the models. Results showed that correlation analysis could eliminate the irrelevant variables, but could not remove the variables with dependence relation.

Considering that the variables of the regression had to be really independent from each other, path analysis was carried out. Estimates of direct and indirect path coefficient were presented in Table 2. The elements in the last column were the significances of variables in tomato and pumpkin. The bold diagonal elements were direct path coefficients, and the rest were indirect path coefficients.

| Table 1  Correlation of $CO_2$ exchange and environmental factors in tomato (T) and pumpkin (P) |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
|               | $X_1$          | $X_2$          | $X_3$          | $X_4$          | $X_5$          | $X_6$          | $X_7$          | $X_8$          |
| $X_2$ T       | 0.292          | 0.428          | −0.058         | 0.023          | −3.067         | 0.649          | −0.007         | *              |
| P             | −1.263         | 0.855          | −0.575         | −0.390         | −2.757         | 1.925          | 0.004          |                |
| $X_3$ T       | −1.966         | −0.348         | −0.796         | 0.171          | −0.018         | 3.548          | −1.434         | 0.001          |
| P             | 1.208          | −0.493         | 0.268          | 0.338          | 0.314          | −0.765         | −0.017         | **             |
| $X_4$ T       | 1.879          | 0.320          | 0.867          | −0.140         | 0.017          | −3.311         | 1.292          | −0.000         |
| P             | −1.268         | 0.540          | −0.335         | −0.289         | −0.297         | 1.040          | 0.029          | ***            |
| $X_5$ T       | 0.552          | −0.240         | −0.489         | 0.248          | −0.002         | 2.401          | −1.656         | −0.007         |
| P             | −1.432         | 0.697          | 0.285          | 0.642          | −0.313         | 2.146          | −2.146         | −0.007         |
| $X_6$ T       | −2.065         | −0.248         | −0.571         | 0.017          | −0.026         | 2.517          | −0.422         | 0.005          |
| P             | 1.330          | −1.208         | −0.334         | 0.429          | 0.468          | 0.603          | 0.103          | 0.012          |
| $X_7$ T       | 2.015          | 0.347          | 0.806          | −0.167         | 0.018          | −3.561         | 1.395          | −0.001         |
| P             | −1.358         | 1.623          | 0.495          | 0.374          | −0.359         | −0.324         | 1.103          | 0.012          |
| $X_8$ T       | −0.855         | −0.281         | −0.631         | 0.231          | −0.006         | 2.798          | −1.776         | −0.006         |
| P             | −1.401         | 0.582          | 0.256          | −0.627         | −0.306         | −0.163         | 2.196          | −0.006         |
|               | −0.664         | −0.010         | −0.011         | −0.067         | −0.005         | 0.168          | 0.427          | 0.026          |
|               | −0.088         | 0.428          | 0.239          | 0.071          | 0.114          | −0.058         | −0.199         | 0.065          |

Note: * $p<0.05$; ** $p<0.01$; *** $p<0.001$.

| Table 2  Path analysis of $CO_2$ exchange and environmental factors in tomato (T) and pumpkin (P) |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
|               | $X_1$          | $X_2$          | $X_3$          | $X_4$          | $X_5$          | $X_6$          | $X_7$          | $X_8$          |
| $X_2$ T       | 2.340          | 0.292          | 0.696          | −0.058         | 0.023          | −3.067         | 0.649          | −0.007         |
| P             | −1.598         | 1.263          | 0.428          | −0.575         | −0.390         | −2.757         | 1.925          | 0.004          |
| $X_3$ T       | −1.966         | −0.348         | −0.796         | 0.171          | −0.018         | 3.548          | −1.434         | 0.001          |
| P             | 1.208          | −0.493         | 0.268          | 0.338          | 0.314          | −0.765         | −0.017         | **             |
| $X_4$ T       | 1.879          | 0.320          | 0.867          | −0.140         | 0.017          | −3.311         | 1.292          | −0.000         |
| P             | −1.268         | 0.540          | −0.335         | −0.289         | −0.297         | 1.040          | 0.029          | ***            |
| $X_5$ T       | 0.552          | −0.240         | −0.489         | 0.248          | −0.002         | 2.401          | −1.656         | −0.007         |
| P             | −1.432         | 0.697          | 0.285          | 0.642          | −0.313         | 2.146          | −2.146         | −0.007         |
| $X_6$ T       | −2.065         | −0.248         | −0.571         | 0.017          | −0.026         | 2.517          | −0.422         | 0.005          |
| P             | 1.330          | −1.208         | −0.334         | 0.429          | 0.468          | 0.603          | 0.103          | 0.012          |
| $X_7$ T       | 2.015          | 0.347          | 0.806          | −0.167         | 0.018          | −3.561         | 1.395          | −0.001         |
| P             | −1.358         | 1.623          | 0.495          | 0.374          | −0.359         | −0.324         | 1.103          | 0.012          |
| $X_8$ T       | −0.855         | −0.281         | −0.631         | 0.231          | −0.006         | 2.798          | −1.776         | −0.006         |
| P             | −1.401         | 0.582          | 0.256          | −0.627         | −0.306         | −0.163         | 2.196          | −0.006         |
|               | −0.664         | −0.010         | −0.011         | −0.067         | −0.005         | 0.168          | 0.427          | 0.026          |
|               | −0.088         | 0.428          | 0.239          | 0.071          | 0.114          | −0.058         | −0.199         | 0.065          |

Note: * $p<0.1$; ** $p<0.05$; *** $p<0.01$. 
From the information in Table 2, the results of path analysis in tomato showed that \( T_a, R_a, V_{pd} \) and \( D_p \) had direct effect on \( E \), and the significances were also great. While \( R_{II}, R_a, A_{II}, C_{CO_2} \) showed notability influence in pumpkin.

Therefore, path analysis could not only reflect the relation between independent variables and dependent variable, but also eliminate the variables with dependence relation. The path analysis could help to further identify the unwanted independent variables caused by couplings, measuring error, and accidental factors, especially when sample data was small.

### 3.2 Regression modeling

According to the results of multivariate analysis, impact factors were picked out as the independent variable. The multivariate regression equation was found using these parameters and \( E \). The comparison of four models’ performance on complexity and accuracy was shown in Table 3. Here the aggregative indicator calculated by Equation (8) was used to measure performance of each model.

From Table 3, the linear model was the simplest model, but its accuracy was the worst, because of its largest error. Although the accuracy of full quadratic model was the best, this model had the most coefficients. The accuracy of pure quadratic, interaction and full quadratic models were similar, and the pure quadratic model had the substantially lower complexity than others. Overall, pure quadratic was the most optimal model among the four models because that its aggregative indicator was the smallest.

### 3.3 Modeling and verification

Since the experimental results of tomato and pumpkin showed that path analysis and pure quadratic were the optimal methods of analysis and modeling, we use the data of cucumber to verify the conclusion. The monitored data of cucumber were divided into two parts, the first 48 groups of which were sampled data for modeling, and the rest were test data. Using the modeling data of cucumber, we used path analysis to analyze the influence among the variables. The result was shown in Table 4.

<table>
<thead>
<tr>
<th>( X_1 )</th>
<th>( X_2 )</th>
<th>( X_3 )</th>
<th>( X_4 )</th>
<th>( X_5 )</th>
<th>( X_6 )</th>
<th>( X_7 )</th>
<th>( X_8 )</th>
<th>Sig.</th>
</tr>
</thead>
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<td>3.043559</td>
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</tr>
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</tr>
<tr>
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<tr>
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<td>-0.2081</td>
<td>0.142055</td>
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<td>1.338523</td>
<td>-0.1136</td>
<td>**</td>
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<td>1.870796</td>
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<td>-0.57964</td>
<td>-0.3572</td>
<td>0.139326</td>
<td>*</td>
</tr>
</tbody>
</table>

Note: *\( p<0.1; ** p<0.05; *** p<0.01.\)

From Table 4, \( R_a \) had great impact on \( CO_2 \) exchange, \( V_{pd} \) had impact, and both \( T_a \) and \( D_p \) had little impact. Then the environmental characters related to \( CO_2 \) exchange, containing \( T_{in}, R_{a}, V_{pd} \) and \( D_p \) were obtained by the method of path analysis. And the results were consistent with that in tomato. On the basis of that, we found four regression equations, and the comparison of four equations’ performance on complexity and accuracy was in Table 5.

<table>
<thead>
<tr>
<th>( X_1 )</th>
<th>( X_2 )</th>
<th>( X_3 )</th>
<th>( X_4 )</th>
<th>( X_5 )</th>
<th>( X_6 )</th>
<th>( X_7 )</th>
<th>( X_8 )</th>
<th>Sig.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear</td>
<td>Pure quadratic</td>
<td>Interaction</td>
<td>Quadratic</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>RMSE</td>
<td>0.1169126</td>
<td>0.0709691</td>
<td>0.0703446</td>
<td>0.0715963</td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>P</td>
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<td>0.084806</td>
<td>0.087762</td>
<td>0.083788</td>
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</tr>
<tr>
<td>Accuracy</td>
<td>MAE</td>
<td>0.4092002</td>
<td>0.2265184</td>
<td>0.2250922</td>
<td>0.2162365</td>
<td></td>
<td></td>
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3.3 Modeling and verification

Since the experimental results of tomato and pumpkin showed that path analysis and pure quadratic were the optimal methods of analysis and modeling, we use the data of cucumber to verify the conclusion. The monitored data of cucumber were divided into two parts, the first 48 groups of which were sampled data for modeling, and the rest were test data. Using the modeling data of cucumber, we used path analysis to analyze the influence among the variables. The result was shown in Table 4.
The results in Table 5 show consistency with those in Table 3. The linear equation’s accuracy was the worst. And full quadratic equation was so complex that it not suitable for modeling. Besides, the errors of pure quadratic and interaction equations were similar. But the pure quadratic equation was simpler than interaction equation. The aggregative indicator of pure quadratic equation was the smallest, and that indicated the model showed the best comprehensive performance.

Otherwise substituting the predicted data of cucumber into the fitting regression equations, the ordinate was CO₂ exchange in terms of time. The comparison of predicted results of four regression equations was shown in Figure 3.

Figure 3  Comparison of predicted results of four multivariate regression models

The results shown in Figure 3 indicated that the error of pure quadratic model was obviously the smallest. And the next best model was linear model. In addition, the accuracies of interaction and full quadratic models were worse, compared with the linear and pure quadratic model. The error of interaction model increased rapidly after 6:00 am, and there was the fluctuation in the curve of full quadratic model after 3:00. The CO₂ exchange rate of photosynthesis was much larger than that of the respiration, especially if the radiation was enough. So the absolute error rose significantly in the morning, while the relative error might vary more smoothly. What more, the accuracy would usually be high, if the monitoring time of testing data was close towards that of the sample data. There were over 10 hours from the last 22:00 to 9:00. The period was so long that interaction and full quadratic models could not predict very accurately.

4 Conclusions

This research took tomato, pumpkin and cucumber as examples to study the optimal methods of multivariate statistical analysis and regression, to avoid the blindness in crop modeling. According to the analyzed results of tomato and pumpkin, path analysis was more suitable to for multivariate statistical analysis than correlation analysis, because it could not only express comprehensively the inner influence between variables, but also eliminate the variables with dependence relation. In the analysis process of regression model, an aggregative indicator was put forward, taking account of two aspects including accuracy and complexity comprehensively. From the comparison between four multivariate binomial regression models, the pure quadratic model had advantages over the others in comprehensive performance. The results of cucumber verified that path analysis and pure quadratic model were suitable for statistical analysis and regression in crop modeling. However, the accuracy of the model was not good enough during the last three hours. That showed the methods could only be applied for short-term prediction if the sample was little.

All in all, through the comparison of common statistical analysis and regression model, we verified the better performance of path analysis and pure quadratic model. The research could offer reference for crop modeling with small sample size, by the comparison of methods of multivariate analysis and regression. The results can not only be used in modeling of CO₂ exchange rate, but also extend to the modeling of other ecological and physiological characteristics in other crops.

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