Inertial force balance and ADAMS simulation of the oscillating sieve and return pan of a rice combine harvester

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Abstract: To reduce the inertial force of the oscillating sieve and return pan of a rice combine harvester, partial equilibrium was adopted. Firstly, based on the kinematic analysis of a slider-crank mechanism, the appropriate mass of counterweight intervals was achieved. Then, an ADAMS dynamic simulation was used to determine the optimum balance mass of the oscillating sieve and return pan individually. Considering the relative motion between the return pan and the oscillating sieve, the overall inertial force of the two parts would be reduced. The simulation results indicated that the optimum counterweight of the oscillating sieve was 15.5 kg based on an analysis of the movement tracks of the mass center and overall inertial force. The results also showed that the overall balance of inertial force not only reduced the counterweight but also decreased the overall inertial force of the oscillating sieve and return pan. Finally, a search for the most suitable crank initial angle of the return pan to reduce the overall inertial force and optimize the overall balance revealed three groups of initial angles: $\phi$=0°, $\phi$=45°, and $\phi$=90°. The results indicated that arranging the initial angle of the crank of the oscillating sieve and return pan in the same position ($\phi$=90°) was the most favorable for reducing the overall inertial force. In this situation, the optimum counterweight of the oscillating sieve was only 14.0 kg. The results can provide references for the design of the overall balance of the inertial force in the cleaning components of a combine harvester.

Keywords: rice combine harvester, oscillating sieve, return pan, inertial force balance, ADAMS
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1 Introduction

During the cleaning process of a rice combine harvester, the oscillating sieve and return pan are influenced by the inertial force of rotary motion in addition to external loads. The inertial force affects the frame and other parts of the combine harvester, which can lead to strong vibration and noise directly influencing the reliability and service life of a combine harvester.[1-3] It is necessary to reduce the impact of the inertial force of the oscillating sieve and return pan as much as possible. Complete balance and partial equilibrium are the main two methods used to balance the inertial force[4]; however, complete balance is not a suitable method for the oscillating sieve or return pan because the counterweight may outweigh the mechanism itself and the interference caused by the counterweight can thus directly or indirectly affect the normal functioning of other parts[5]. Even if the oscillating sieve could achieve complete balance, this complete balance would lead to input torque, causing the counter-force of the connecting frame pair to increase considerably[6]. Therefore, considering the actual structure of the oscillating sieve and the return pan, the partial equilibrium method is more practical.

The main research on the inertial force balance includes the following: According to Chaudhary et al.[7], the shaking forces and shaking moments developed as a result of inertial forces in mechanisms were minimized using the genetic algorithm (GA), which was found to be better than the conventional optimization algorithm results. Arakelian et al.[8] adopted two symmetric sliders to balance the inertial force and reduce the shock torque by adjusting the parameters of the connecting rod. The inertial force and inertial torque of the slider-crank were balanced by adding a cam mechanism by reversing the crank, and the torque of the mechanism was compensated for by the spring. Research on the inertial balance force on a combine harvester includes the following: Guarnieri et al.[9] noted that the imbalance between the reciprocating single-blade cutter bar and the slider-crank mechanism was due more to the periodic instability of motion and torque than to the alternative inertial force of the blade; the paper also showed the existence of an optimum running speed that minimizes instability to understand the vibration characteristics of the knife-driving system. To reduce the vibration of a rice combine harvester, mechanisms of the knife-driving system were examined according to the trajectory based on the frequency components and the correlation of each frequency band using analyzed recurrence plots[10]. Somchais[11] studied three types of new cutter bar drivers: stir type, perpendicular axis type driven by a chain, and perpendicular axis type driven by a belt; the vibration of the header tended to be lowest when the perpendicular axis type driven by a chain was used. Li et al.[12] performed a finite element analysis of a connecting rod with Solidworks software and optimized the structure with DOE (design of experiments).
technology. Based on the kinematic and dynamic modes of a crank slide-type oscillating sieve, the inertial force of the oscillating sieve was obtained and optimized using Matlab\(^\text{[13]}\).

The above related research obtained specific results on reducing the inertial force of a slider-crank mechanism and other parts of a combine harvester. However, with respect to balancing an oscillating sieve, the research only optimized the inertial force equation or only adopted a simplified model of the slider-crank mechanism to simulate the oscillating sieve, resulting in a large error between the theoretical counterweight and practical counterweight. In addition, no relevant papers on the inertial force offset and simulation of the oscillating sieve and return pan as a whole have been published to date. The above studies ignored the inertial force offset of the two parts in the process of mutual movement; as a result, the counterweight was not the actual optimal balance weight.

In this study, partial equilibrium of the inertial force balance was used to calculate the counterweight intervals of the slider-crank mechanism and the optimum mass in the counterweight interval obtained with ADAMS software. Based on a comprehensive consideration of the relative motion of the oscillating sieve and the return pan, the optimum mass for the overall balance of two devices was obtained, providing a design method for the counterweight that addresses the inertial force reduction of the oscillating sieve and return pan.

2 Materials and methods

2.1 Working principle of the oscillating sieve and return pan

To address the harvesting requirements for high-yield rice, a new type of threshing and cleaning system was developed, composed of a transverse tangential thresher, a longitudinal rotor, a multi-duct fan and a double-layer oscillating sieve\(^\text{[14]}\), as shown in Figure 1. The tangential thresher is used to thresh mature and easily threshed rice kernels, and the remaining kernels in the panicles are threshed by the longitudinal rotor. The mixture from the tangential and longitudinal concaves includes kernels, short straw, and light materials. The fan has to generate an even airflow with proper air speed over the sieves to separate grain kernels from straw and chaff, collectively known as material other than grain (MOG)\(^\text{[15]}\).

The mechanical process of the new threshing and cleaning device can be summarized as follows. The mass of composite materials from the tangential threshing cylinder drops into the oscillating pan located in front of the sieve, on which they are progressively deflected toward the front of the upper sieve. Subsequently, the mass of composite materials from the longitudinal axial-flow threshing cylinder drop directly onto the return pan. The combined effects of fan airflow and the oscillating shaker remove light materials from the composite materials from two cylinders to assist in positioning kernels over the sieve openings and moving particles along the sieve surface if they did not pass through the sieve openings. Finally, the clean kernels passing through sieve openings are gathered and conveyed to the tank by the clean grain auger. Some composite materials that do not pass through the sieve openings fall into the tailings auger; they are conveyed to the return pan from the tailing window, while the long straw is conveyed by the oscillating chaffer toward the rear of the combine\(^\text{[16]}\), as shown in Figure 2.

2.2 Dynamic analysis of the oscillating sieve and return pan

Both the oscillating sieve and return pan can be simplified as a slider-crank mechanism\(^\text{[17]}\). Because the crank length is much shorter than the connecting rod length (approximately 1:100), it can be considered that the moving direction of the slider and the rotation center of the crank are in the same straight line. Therefore, the in-line slider-crank mechanism was regarded as the analysis model of the oscillating sieve and the return pan, as shown in Figure 3.

2.2.1 Inertial force and counterweight of the slider-crank mechanism

Assuming the masses of the crank and connecting rod are \(m_1\) and \(m_2\), respectively, that the mass centers are \(S_1\) and \(S_2\), respectively, and that the slider mass is \(m_s\), according to the static mass substitution method, \(m_1\) is replaced with \(m_{A1}\) and \(m_{B1}\), and \(m_2\) are replaced with \(m_{B2}\) and \(m_{C2}\), respectively. Thus, the inertia of the mechanism acts on place \(B\) and place \(C\).
\[ m_0 = m_{b1} + m_{b2} \]
\[ m_4 = m_{c2} + m_{l2} \]

where, \( m_{b1} = \frac{c}{l} m_{b} \), \( m_{b2} = \frac{b}{l} m_{b} \), \( m_{c2} = \frac{a}{l} m_{c} \), and \( m_{l} \) is the mass of the slider.

In this mechanism, the displacement of the slider is as follows:
\[ S = r \cos \theta + l \cos \varphi \]  
(2)

where, \( r \) is the length of the crank; \( \theta \) is the rotation angle of the crank, and \( \varphi \) can be obtained from the trigonometric function relation:
\[ \sin \varphi = \frac{1}{r} \sin \theta = \lambda \sin \theta \text{ and } \cos \varphi = (1 - \lambda^2 \sin^2 \theta)^{\frac{1}{2}}, \]
where \( \lambda \) is the ratio of the crank length and the connecting rod length. \( \cos \varphi \) can expand into the angle \( \theta \) progression; for this mechanism, \( \lambda = 0.01 \) and the high-order terms containing \( \lambda \) can be omitted. To solve the displacement \( S \), the second derivative can be omitted, providing the acceleration of \( C \):
\[ a_c = r \dot{\theta} (\cos \theta + \lambda \cos 2\theta) \]  
(3)

From the above analysis, the rotating inertial force of \( B \) and moving inertial force of \( C \) can be obtained:
\[ F_B = m_B r \dot{\theta}^2 \]  
(4)
\[ F_C = m_C a_c = m_C r \dot{\theta} (\cos \theta + \lambda \cos 2\theta) \]  
(5)

The term \( F_C \) containing \( \cos \theta \) is called the first-order inertial force; the term \( F_C \) containing \( \cos 2\theta \) is called the second-order inertial force. According to the partial equilibrium method, a counterweight (Figure 3) is set at the appropriate reverse distance of the crank and the rotation inertial force \( F_B \) can be balanced by the mass of \( D \):
\[ m_{11} r \dot{\theta}^2 = m_B r \dot{\theta}^2; \text{ thus, } m_{11} = \frac{r}{r'} m_B \]  
(6)

Similarly, to balance the moving inertial force generated in the horizontal direction, a counterweight \( m_{12} \) should also be set; however, that counterweight would exert an unnecessary vertical inertial force, and the second-order inertial force cannot be balanced. In this mechanism, the second-order inertial force is quite small and can thus be ignored. The horizontal inertia and vertical inertial forces caused by \( m_{12} \) are as follows:
\[ F_1 = m_{12} r \dot{\theta} \cos \theta \]
\[ F_2 = m_{12} r \dot{\theta}^2 \sin \theta \]  
(7)

In the present comprehensive analysis, a coefficient \( k \) was used to multiply \( m_{12} \) to balance the horizontal inertial force while the vertical inertial force was not too large. In general, \( k \) is 1/3-1/2.

Based on the above analysis, the counterweight is composed of two parts, \( m_{12} \) and \( k m_{02} \):
\[ m_B = m_{11} + k m_{12} = \frac{r}{r'} (m_B + k m_C) \]  
(8)

2.2.2 Inertial force and counterweight of the oscillating sieve and the return pan

The return pan comprises a roller, vibrating board and eccentric shaking shaft (Figure 4); the eccentric shaking shaft is simplified into a crank, the vibrating board is simplified into a connecting rod, and the roller is simplified into a slider as well. Based on the above calculation of the slider-crank mechanism inertial force and counterweight analysis, the proper counterweight intervals could be combined with the actual data of the oscillating sieve and return pan. The eccentricity of the eccentric shaking shaft was 15 mm, and the mass was 1.0 kg, and the mass center was located at a distance of 12.3 mm from point A; the rotational speed was 350 r/min. The length of the vibrating board was 1045 mm, the mass center was located at a distance of 12.3 mm from point B; the mass of the vibrating board was 23.7 kg, and the mass of the roller was 0.26 kg.

Figure 4 Return pan structure diagram

From the above formulas, the following can be calculated: \( m_{b2} = 11.1 \) kg, \( m_{b1} = 0.8 \) kg, \( m_{c2} = 12.6 \) kg. Thus, \( m_{b} = 11.9 \) kg and \( m_{c} = 12.86 \) kg. The counterweight was installed at the reverse of the crank: \( r' = 45 \) mm, when, \( k = 1/3 \); when \( m_{b1} = 6.1 \) kg, \( k = 1/2 \). Thus, the counterweight intervals of the return pan are 5.4-6.1 kg.

The oscillating sieve comprises an eccentric shaking shaft, a screen board and a roller, as shown in Figure 5.

Figure 5 Oscillating sieve structure diagram

In the slider-crank mechanism model of the oscillating sieve, the crank length is 15 mm, the mass is 1.0 kg, and the mass center is located at a distance of 12.3 mm from point A; the rotational speed is 350 r/min. The length of the connecting rod is 1378 mm, the mass center is located at a distance of 448 mm from point C, and the mass is 90.4 kg. The rolling wheel mass is 0.26 kg. Thus, \( m_{b2} = 29.5 \) kg and \( m_{c2} = 61.26 \) kg. The counterweight of the oscillating sieve was also installed in the reverse of the crank: \( r' = 45 \) mm. Finally, the counterweight intervals of the oscillating sieve are 16.7-20.1 kg.

2.2.3 Overall inertial force balance of the oscillating sieve and the return pan

During the working process of the oscillating sieve and the return pan, the crank shaft is driven to rotate by a chain reverse wrapped around a chain wheel, with the cranks of the oscillating sieve and the return pan rotating in opposite directions. Therefore, in the balance of the inertial force of the oscillating sieve and the return pan, the mutual movement relationship between the two mechanisms should be considered, and for the whole mechanism, the rotation directions of the two cranks are opposite and thus the overall inertial force of the two parts can be reduced. This feature can be utilized to reduce the counterweight mass of the oscillating sieve, steady the operation of the mechanism and reduce the input torque and energy consumption.

The inertial force analysis of the return pan showed that the mass of the slider-crank mechanism was replaced by the combined masses of \( B \) and \( C \); then, the inertial force balance was achieved by
setting the counterbalance. According to the same principle, when the overall balance was taken into account, the mass of the return pan was replaced with the combined masses B and C, and the mass of the oscillating sieve was replaced with the combined masses of B’ and C’, as shown in Figure 6.

Figure 6 Schematic showing the oscillating sieve and return pan mechanism

The moving inertial force generated by mass C and C’ is as follows:

\[
\begin{align*}
F_c &= m_c \omega(t)^2 \cos \theta_1 \\
F_c' &= m_c' \omega(t)^2 \cos \theta_2
\end{align*}
\]  

(9)

where, \( \cos \theta_1 = \cos(\omega t + \phi) \), \( \cos \theta_2 = \cos(\omega t + 90^\circ) \), and \( \phi \) is an arbitrary initial angle.

According to Equation (9), the moving inertial force generated by mass C and C’ could be reduced in the movement. The following discussion is about how to obtain the most suitable initial angle of the return pan’s crank to minimize the overall inertial force of the oscillating sieve and return pan when the initial phase of the oscillating sieve is 90° because of structural design requirements.

The resultant force from the inertial force in the horizontal direction (X direction) of the oscillating sieve and return pan system is as follows:

\[
F_{cc} = r \omega^2 (m_c \cos \theta_1 + m_c' \cos \theta_2)
\]  

(10)

In one cycle, the average moving inertial force was compared with the average moving inertial force without considering the inertial force offset:

\[
\eta_1 = \frac{1}{T} \int_0^T F_{cc} \, dt
\]  

(11)

Inserting the data into the formulas provides the following conclusions:

1) when \( \phi=45^\circ \), \( \eta_1=0.72 \), and \( \eta_2=0.86 \), both moving inertial force and rotating inertial force were reduced to some degree based on the balance of the inertia and according to the above formulas. The counterweight mass of the oscillating sieve was \( m'_{D2}=13.9-16.5 \) kg.

2) when \( \phi=90^\circ \), \( \eta_1=0.65 \), and \( \eta_2=0.71 \), the maximum offset of the inertial force and the overall inertial force was minimal. Thus, \( \phi=90^\circ \) was the most suitable initial angle of the return pan’s crank. According to the above formulas, the counterweight mass of the oscillating sieve was \( m'_{D2}=11.4-13.7 \) kg.

3) when \( \phi=0^\circ \), \( \eta_1=0.74 \), and \( \eta_2=0.77 \), both the moving inertial force and rotating inertial force were reduced to some degree, but the decreased degree of the overall inertial force was less. The counterweight mass of the oscillating sieve was \( m'_{D2}=13.2-15.8 \) kg.

3 Simulation analysis of the oscillating sieve and return pan

3.1 Movement tracks of the mass center and inertial force analysis of the return pan

Based on the definition of the inertial force balance, when the total mass of the mechanism is constant, the greater the acceleration of the mass center, the greater the inertial force. Therefore, in the fixed cycle, the greater the range of motion of the mass center, the greater the acceleration and inertial force. Hence, the target of the inertial force balance is to make the movement range of the mass center as small as possible in one cycle.

To provide a simulation result closer to the actual motion of the mechanism, the assembled model of the return pan was imputed into the ADAMS software, shown in Figure 8. In the ADAMS set as follow: the motion pair between the vibrating board and eccentric shaking shaft was a rotating pair, the motion pair between the counterweight and sprocket wheel was a fixed pair, the motion pair between the roller and guide rails fixed on the frame was a moving pair, and the motion pair between vibrating board and the roller was a rotating pair \( \text{[16]} \). To reflect the influence of the inertial force on the frame, a side board was set as the frame and

\[
\begin{align*}
F_{x1} &= m_{r} \omega(t)^2 \cos \theta_1 \\
F_{x2} &= m_{r} \omega(t)^2 \cos \theta_2
\end{align*}
\]  

(12)

Y direction:

\[
\begin{align*}
F_{y1} &= m_{r} \omega(t)^2 \sin \theta_1 \\
F_{y2} &= m_{r} \omega(t)^2 \sin \theta_2
\end{align*}
\]  

(13)

The resultant forces in the X and Y directions are as follows:

\[
\begin{align*}
F_x &= F_{x1} + F_{x2} \\
F_y &= F_{y1} + F_{y2}
\end{align*}
\]  

(14)

The resultant inertial force of the oscillating sieve and return pan is as follows:

\[
F = \sqrt{F_x^2 + F_y^2}
\]  

(15)

In one cycle, the average resultant rotating inertial force was compared with the average inertial force without considering the inertial force offset:

\[
\eta_2 = \frac{1}{T} \int_0^T \frac{1}{T} \int_0^T F_{cc} \, dt
\]  

(16)
fixed on the ground, and the motion pair between the side board and the eccentric shaking shaft was a rotating pair. During the simulation process, the eccentric shaking shaft speed was 2100 (°)/s (350 r/min).

Figure 8  Simulation model of the return pan in ADAMS

In the counterweight interval (5.4-6.1 kg), four sets of data were selected as the variable: 5.5 kg, 5.7 kg, 5.9 kg and 6.1 kg. The simulation time was 0.5 s, and the step size was 0.01 s. The relationship between the position coordinates of the mass center of the return pan and time was obtained and processed in EXCEL (Figures 9 and 10). The return pan in the Z direction did not have movement displacement; therefore, in the X and Y dimensions, the movement tracks of the mass center were determined, as shown in Figures 11 and 12.

Figure 9  Displacement of the mass center in the X direction

Figure 10  Displacement of the mass center in the Y direction

Figure 11  Movement tracks of the mass center under different counterweights

In the simulation process, different counterweight settings would change the mass center stability and balance. The following conclusions can be drawn from Figures 9-12:

(1) The mass center moved in the X and Y directions with 0.17 s of one cycle, the fluctuation in the X direction was larger (14 mm), and that of the Y direction was relatively small (1.1 mm).

(2) Compared with no counterweight, the X displacement decreased from 21.9 mm to 9-11 mm and the Y displacement decreased from 11.1 mm to 0.2-0.6 mm after adding the counterweight.

(3) Different counterweights resulted in different movement tracks of the mass center. When the counterweight was 5.9 kg, the movement tracks range of the mass center reached its minimum of 1.7 mm². The corresponding balance effect was also optimal. Thus, it can be concluded that the optimum counterweight was 5.9 kg.

In the above images, a reflection of the inertial force changes through the movement tracks of the mass center was intuitive but cannot accurately show the specific numerical value of the inertial force. If the counterweight is in inappropriate position, it may cause excessive force on the motion pair. Specifically, at the bearing connecting the crank and frame, the bearing may be damaged because of the impact and is thus not conducive to balancing the return pan. Thus, it was necessary to calculate the inertial force of the return pan. Through the ADAMS/Postprocessor, the counter-force in the X and Y directions at joints (Figures 13 and 14, respectively) is shown and the inertial force is obtained under different counterweights, as shown in Figure 15.

From Figures 13-15 and Table 1, the following can be concluded:

(1) Compared with no counterweight (red curve in figures), the peak-to-peak value of the counter-force in the X direction decreased from 850 N to 1408 N after the addition of counterweights and the peak-to-peak value of the counter-force in the Y direction decreased from 586 N to 275 N. The degree of reduction was substantial, showing that the counterweight achieved the balance of the inertial force.

(2) Compared with no counterweight, after the addition of counterweights, the mean value, RMS, and peak-to-peak values all decreased greatly, proving the effectiveness of achieving partial equilibrium by setting the counterweight.

(3) In the four counterweight sets, when the mass of the counterbalance was 5.9 kg, the mean value, RMS, and peak-to-peak values were relatively small. This mass can be considered to be the optimum counterweight of the return pan; this was consistent with the former analysis; when the counterweight was 5.9 kg, the movement tracks range was at a minimum.
Figure 13  Counter-force in the X direction under no counterweight and different counterweight qualities

Figure 14  Counter-force in the Y direction under no counterweight and different counterweight qualities

Figure 15  Inertial force of return pan under no counterweight and different counterweight qualities

Table 1  Inertial force under different counterweight qualities

<table>
<thead>
<tr>
<th>Mass/kg</th>
<th>Min/N</th>
<th>Max/N</th>
<th>Mean value/N</th>
<th>RMS</th>
<th>Peak-to-peak value/N</th>
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3.2 Movement tracks of the mass center and inertial force analysis of the oscillating sieve

Referring to the simulation process of the return pan, in the counterweight interval (16.7-20.1 kg), six sets of data were selected as the variable: 16.8 kg, 17.4 kg, 18.0 kg, 18.6 kg, 19.2 kg and 19.8 kg. The simulation time was 1.0 s, and the step size was 0.01 s. This process also described the movement tracks of the mass center and counter-force (Figures 17 and 18).

Figure 16  Simulation model of the oscillating sieve in ADAMS

Figure 17  Movement tracks of the mass center under different counterweights

Figure 18  Movement tracks of the mass center under different counterweights compared with no counterweight
As shown in Table 3, when the counterweight was 15.5 kg, the movement track range of the total mass center was at a minimum and the peak-to-peak value was also at a minimum. Thus, the optimum counterweight of the overall balance was 15.5 kg.

### Table 3 Overall inertial forces under different counterweights

<table>
<thead>
<tr>
<th>Mass/kg</th>
<th>Min/N</th>
<th>Max/N</th>
<th>Mean value/N</th>
<th>RMS</th>
<th>Peak-to-peak value/N</th>
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<td>1568</td>
<td>2530</td>
<td>1925</td>
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</table>

Figure 21 shows that when the overall balance counterweight was 15.5 kg, the movement track range of the mass center was smaller than the movement track range with a 18 kg counterweight, which was the optimum counterweight in the above. It was concluded that, the overall balance not only reduced the counterweight but also made the oscillating sieve and return pan more balanced according to the above method.

Crank initial angle of the return pan was another important factor in the overall balance when crank initial angles of the oscillating sieve were immutuable; different crank initial angles of the return pan will cause different degrees of inertial force offset. According to Figure 22, the main movement of the oscillating sieve and return pan and the inertial force on the frame were mainly in the X direction. With $\phi=45^\circ$, although the inertial force decreased and the counterweight was smaller, the inertial force offset in the X direction was still not ideal and the overall inertial force was relatively large. Therefore, three different crank initial angle ($\phi=0^\circ$, $\phi=45^\circ$ and $\phi=90^\circ$) of the return pan were set up in the ADAMS to find the optimum angle that minimize the overall inertia force.

The analysis showed that: when $\phi=90^\circ$ (the crank initial angle of the return pan was the same as the crank initial phase of the oscillating sieve), the degree of inertial force offset in the X direction was at a maximum and the overall inertia was at a minimum (Figure 23). Figure 24 showed the different initial angles of the crank of the return pan in ADAMS.

Figure 25 shows that the maximum and minimum values of the overall inertial force were 2518 N and 1611 N with $\phi=45^\circ$, 1604 N and 613 N with $\phi=90^\circ$, 1828 N and 697 N with $\phi=0^\circ$, respectively. When $\phi=90^\circ$, both the maximum and the minimum were

### Figure 20 Movement tracks of the mass center under different counterweights

Table 2 Inertial force under different counterweights

<table>
<thead>
<tr>
<th>Mass/kg</th>
<th>Min/N</th>
<th>Max/N</th>
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<td>19.8</td>
<td>792</td>
<td>2070</td>
<td>1424</td>
<td>1484</td>
<td>1278</td>
</tr>
</tbody>
</table>

Compared with no counterweight, the movement track range of the mass center was relatively small (Figure 18). After the addition of the counterweight, the movement track range of the mass center under different counterweights was similar, as shown in Figure 17. Hence, the following was the optimum counterweight obtained from comparing the counter-force.

From Figures 17-18 and Table 2, the following can be concluded:

1. Compared with no counterweight, the movement track range markedly decreased after the addition of the counterweight, showing not only that the inertial force of the oscillating sieve was significantly decreased but also that it produced a meaningful balance effect.

2. When the counterweight was 18.0 kg, the peak-to-peak value was not the smallest, but the analysis of the RMS and mean value showed that 18.0 kg was a better counterweight. Hence, 18.0 kg was chosen as the optimum counterweight.

### 3.3 Simulation of the overall inertial force balance

The overall balance model of the oscillating sieve and the return pan is shown in Figure 19. When the overall balance is taken into account, the counterweight of the oscillating sieve can be reduced because of the offset of the inertial force from the return pan.

When $\phi=45^\circ$, in the counterweight interval (13.9-16.5 kg), seven sets of data were selected as the variable: 13.5 kg, 14.0 kg, 14.5 kg, 15.5 kg, 16 kg and 16.6 kg. The simulation time was 1.0 s, and the step size was 0.01 s. After data processing, the movement track of the total center of mass was obtained (Figure 20). The overall counter-force is shown in Table 3.

### Figure 19 Overall balance model in ADAMS

### Figure 20 Movement tracks of the mass center under different counterweights
significantly decreased compared with other initial crank angles, demonstrating that the configuration of the initial crank angle of the oscillating sieve and the return pan at the same position ($\phi=90^\circ$) was the most favorable for reducing the overall inertial force.

**Figure 22** Inertial force offset in the $X$ direction of the return pan and oscillating sieve ($\phi=45^\circ$)

**Figure 23** Inertial force offset in the $X$ direction of the return pan and oscillating sieve ($\phi=90^\circ$)

**Figure 24** Different crank initial angles of the return pan

**Figure 25** Overall inertial force under different crank initial angles of the return pan

### 4 Conclusions

1) The partial equilibrium of the inertial force balance was used to calculate the counterweight intervals of 5.4-6.1 kg for the return pan and 16.0-20.1 kg for the oscillating sieve.

2) The assembled model of the oscillating sieve and return pan were imputed into the ADAMS software individually, and the optimum counterweights were 5.9 kg and 18 kg for the return pan and oscillating sieve, respectively.

3) On the basis of the overall inertial force balance, the simulation results indicated that the optimum counterweight of the overall balance was 15.5 kg based on an analysis of the movement tracks of the mass center and inertial force.
4) The configuration of the initial crank angle of the oscillating sieve and the return pan at the same position (φ=90°) was the most reasonable for reducing the overall inertial force.

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[References]